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Abstract:
This paper compares the distributional effects of conventional monetary policy and quantitative easing (QE) within an estimated open-economy DSGE model of the euro area. The model includes two groups of households: (i) wealthier households, who own financial assets and are able to smooth consumption over time, and (ii) poorer households, who only receive labor and transfer income and live ‘hand to mouth’. We use the model to compare the impact of policy shocks on constructed measures of income and wealth inequality (net disposable income, net asset position, and relative per-capita income). Except for the short term, expansionary conventional policy and QE shocks tend to mitigate income and wealth inequality between the two population groups. In light of the coarse dichotomy of households that abstracts from richer income and wealth dynamics at the individual level, the analysis emphasizes the functional distribution of income.

Keywords: Bayesian estimation, distributional effects, open-economy DSGE model, portfolio rebalancing, quantitative easing.


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1. Introduction

In the context of (risen awareness of) persistent, or even increasing, income and wealth inequality, distributional effects of economic policy occupy a prominent place in policy discussions these days. This is true particularly for structural policies and for fiscal measures, which often have an explicit redistributive aspect. In the context and aftermath of the financial crisis, however, the distributional implications of monetary policy have likewise received more attention.

The distributional effects of monetary policy have received particular attention in the context of large-scale asset purchases (‘quantitative easing’). Especially the link between quantitative easing (QE) and asset prices has nurtured the view that QE has predominantly benefitted wealthy asset owners. A more thorough analysis should however also include other effects of QE, notably its stabilising impact on economic activity, employment, and wage incomes, which remains a central motivation behind the policy.

In this paper, we compare the distributional effects of two monetary policy regimes in a general equilibrium framework: (i) conventional monetary policy, where the central bank follows a Taylor rule to set short-term nominal interest rates, and (ii) QE, where the central bank expands its balance sheet by purchasing long-term government bonds from the private sector. Our analysis builds on the estimated DSGE model of Hohberger et al. (2018), which introduces elements to study the macroeconomic implications of the European Central Bank’s quantitative easing policies. The model distinguishes between two types of households: (i) households that hold assets (government bonds, firm equity, and foreign bonds) and receive related income in addition to wages and transfers, and (ii) households that only receive wage and transfer income. Households (i) can smooth disposable income and consumption over time through financial markets, i.e. they do not face binding liquidity constraints (therefore, they are labelled NLC). Households (ii) live hand-to-mouth, i.e. they face binding liquidity constraints (therefore, they are labelled LC). Given the additional source of income from financial assets (bonds and equity), NLC households are wealthier than LC households.

We compare distributional effects of the two forms of monetary policy between the two household groups embedded in the model and study the impulse responses for a number of constructed distributional measures: the net disposable income, the net asset positions (financial wealth), and the per-capita net disposable income relative to the population average. Given the model's focus on asset owners versus households without financial assets, the analysis concentrates on the impact
of monetary policy on different functional income groups (labor income versus asset returns), rather than providing a more disaggregated perspective on heterogeneity in portfolio holding and associated portfolio valuation and investment income effects within the group of NLC households. The analysis is conducted using a two-region DSGE model for the euro area (EA) and the rest of the world (RoW), estimated with Bayesian techniques. Our model belongs to the class of two-agent New Keynesian (TANK) models, which can be thought of as a tractable middle ground between the (one) representative-agent New Keynesian framework and the heterogeneous-agent New Keynesian (HANK) model of, e.g., Kaplan et al. (2017). Our setup makes two simplifying assumptions compared to HANK models. First, the population shares of the two household types are constant, i.e. invariant to shocks. Second, we abstract from idiosyncratic income risk, which eliminates precautionary saving motives. Recent work by Debortoli and Galí (2018) shows that, despite these differences, the aggregate transmission of a monetary policy shock in TANK models is similar to that in a comparable HANK setup.

The focus of this paper is on the relative position of two groups of households. Arguably, the LC household with labor and transfer income only approximates the income dynamics for the poorer part of the population, whereas intertemporally optimizing bond and equity holders (NLC) represent the wealthier share of the population. Focusing on only two household aggregates, rather than a more detailed income distribution is a price to pay at present for having a model that is richer in other dimensions and feedback mechanisms, such as a larger set of asset types (bonds of different maturities, foreign bonds, and corporate equity) and economic openness, and estimated.

We model QE by incorporating a central bank balance sheet and by distinguishing between short-term and long-term government debt. We use a formulation of private-sector portfolio composition as in Andrés et al. (2004), and Priftis and Vogel (2016), which breaks neutrality of central bank balance sheet policies, notably a change in the maturity structure, by introducing imperfect substitutability between assets of different maturity. The approach is similar to the ‘preferred habitat’ investor framework of Vayanos and Vila (2009) who provide a theoretical model for a duration risk channel of QE. The ‘preferred habitat’ model incorporates two agents: one has preferences for assets of a particular maturity, generating a downward sloping demand curve for that asset; the second agent is an arbitrageur, investing in all assets. In equilibrium, changes in the supply of an asset of particular maturity affect the price of that asset, and, by arbitrage, also the prices of other assets. QE can reduce the duration risk in the hands of investors and alter the yield
curve. Neely (2015) shows that a portfolio choice model can reproduce observed changes in US and foreign bond yields and the USD exchange rate in the context of US QE. Greenwood and Vayanos (2014) examine empirically how the supply and maturity structure of government debt can affect bond yields and expected returns. When controlling for the short-term rate, they find that the maturity-weighted debt-to-GDP ratio is positively associated with bond yields and future returns.

In our framework of modelling QE, the central bank expands its balance sheet by purchasing long-term bonds, the latter modelled as in Woodford (2001), and injecting liquidity to the private sector. Our specification allows us to capture effects of QE through a large number of transmission channels put forward by the literature, e.g. Krishnamurthy and Vissing-Jorgensen (2011), including the saving, financing cost, exchange rate, inflation, and fiscal channels. Lutz (2015) adds an investor sentiment channel, i.e. conventional and unconventional monetary policy shocks affecting investor sentiment or confidence. This channel is present in our model (only) as far as expansionary monetary policy is likely to improve the economic outlook, which in turn affects investment decisions by forward-looking agents.

The analysis in this paper suggests that, similar to conventional short-term interest rate cuts, expansionary QE measures do not increase income and wealth inequality between population groups in our two-household model persistently. Conventional policy and QE policy shocks have a similar impact on real GDP, inflation, employment and the real exchange rate. In both cases, the wage share falls on impact, as wage stickiness raises firm profits, before it returns to baseline and positive territory in the medium term. The net income share of LC households falls on impact, due to the decline in the wage share and the increase in firm profits. In the medium term, when wages catch up, the income share of the LC households, i.e. the poorer part of the population, increases to above baseline. The income share of NLC households, as a mirror image, declines in response to expansionary monetary shocks in our model. The decline is more pronounced and more persistent for the QE shock, which follows from the reduction in private sector long-term bond holdings and associated returns. Looking at relative per-capita disposable income also indicates a (moderate) decline in income inequality in response to expansionary policy shocks.

The net asset position of NLC households at market value increases on impact in our two scenarios, as lower interest rates are associated with an increase in the value of bonds (valuation effects). In the medium term, QE reduces the net asset position of the NLC households. The wealth
decumulation relative to the no-policy baseline follows from the decline in the NLC households' holding of interest-bearing long-term bonds and the reduction in private sector savings for a protracted period.

The remainder of the paper presents a short literature review in Section 2. Section 3 outlines the elements of the model specific to the analysis of quantitative easing and the distributional effects of monetary policy. Section 4 describes the model solution and estimation methodology. Section 5 discusses the impact of conventional and QE shocks on the economy and their distributional effects. Section 6 summarizes the paper and concludes.

2. Related literature on the distributional effects of monetary policy

Economic research has investigated the effect of monetary policy on aggregate economic variables, including total output, employment, and inflation, widely for many decades. In contrast, the theoretical and empirical literature investigating the distributional effects of monetary policy is relatively new.

The existing literature discusses a number of channels that can generate distributional effects of monetary policy and, as a natural extension, of QE. Coibion et al. (2017) summarize these channels. The income composition channel is a first channel affecting the income distribution following monetary policy shocks. This derives from changes in the primary sources of income (e.g., business, financial and labor income, and transfers), which is heterogeneous across households. If expansionary policy, be it a reduction in the short-term interest rate, or purchases of long-term government bonds by the central bank, affects profits, asset returns, wages, or benefits and transfers asymmetrically, different household types will be affected to varying degrees.

A second channel discussed by Coibion et al. (2017) is financial segmentation in the sense that financially more connected traders in financial markets will react faster to changes in monetary policy than the less-connected agents and will therefore benefit at the expense of the latter. This channel refers to distributional effects within the group of financial investors.

The third channel listed in Coibion et al. (2017) is the portfolio channel. Households with disproportionately large net asset positions may gain from expansionary (conventional or unconventional) monetary policy through valuation gains. They may also lose, however, if their assets are not protected against inflation, as in the case of currency. If expansionary policy raises inflation, it erodes the real value of assets with fixed nominal value.
The fourth channel in the list is labelled *savings redistribution* channel and captures the fact that unanticipated expansionary monetary policy, creating surprise inflation, will hurt creditors (savers) and benefit debtors (borrowers) if debt is determined in nominal terms. If creditors and debtors belong to different parts of the wealth distribution, wealth inequality may decline. Finally, Coibion et al. (2017) mention the *earnings heterogeneity* channel. This channel relates to differences in income and unemployment risks across different segments of the labor market. When labor income risk in a recession is stronger in the lower part of the wage distribution, as documented by Heathcote et al. (2010), stabilization policy helps reducing pro-cyclical income dispersion. Colciago et al. (2018) survey empirical studies on the distributional effects of monetary policy. The empirical research on the effect of conventional monetary policy on income and wealth inequality gives mixed results. Furceri et al. (2018) in a recent study find expansionary (contractionary) conventional policy shocks to reduce (increase) *income* inequality in a panel of 32 countries. Coibion et al. (2017) study US monetary policy and find analogously that contractionary monetary policy increases labor and total income inequality. Domanski et al. (2016) use simulations of household finance surveys from five European countries and the US to find that changes in *wealth* inequality since 2009 have been driven by movements in equity valuations and house prices. As real estate is relatively more important at the lower end of the wealth distribution, house price increases alone tend to reduce inequality, whereas increases in equity price, possibly in response to a monetary expansion, tend to increase wealth inequality. Similarly, O’Farrell and Rawdanowicz (2017) stress the uneven distribution of asset classes across the wealth distribution, so that distributional effects depend on which types of asset prices change most. Adam and Tzamourani (2016) use the Household Finance and Consumption Survey (HFCS) to show that the effect of asset price inflation on inequality in euro area countries varies across assets. In particular, changes in bond prices do not have significant effects on inequality, changes in equity prices increase wealth inequality, and changes in house prices reduce inequality. The empirical analysis of distributional effects of unconventional monetary policies, such as QE, faces the difficulty that non-standard policies have been in place for much shorter time, so that time series for longer periods and larger country samples are not readily available at this point. Based on the various transmission channels, Colciago et al. (2018) observe that unconventional monetary policies may reduce income inequality by stimulating economic activity, but may also increase inequality by boosting asset prices. Montecino and Epstein (2015) use data from the Federal
Reserve’s Survey of Consumer Finances and find that recent expansionary unconventional monetary policy in the US contributed to rising inequality, driven in particular by an increase in the value of corporate equities. In line with the earnings heterogeneity channel, the increase in employment amongst the least wealthy had a redistributive role, but was dampened by falling real wages and difficulties in mortgage refinancing of credit-constrained households. Using detailed micro-level data, Mumtaz and Theophiliopoulou (2017) arrive at similar results for the Bank of England’s QE measures. Saiki and Frost (2014) estimate a VAR with household survey data and find that the expansionary non-standard monetary policy in Japan has widened income inequality in the late 2000s, due largely to the portfolio channel. Focusing on the euro area, Guerello (2018) estimates a panel VAR with monetary policy indicators and measures of income inequality. Her results suggest high cross-country heterogeneity in the impact of monetary policy and interactions with the redistributive strength of fiscal policy and the maturity of the household portfolio. She finds that unconventional monetary policy tends to increase income inequality the more wealth is stored in financial assets rather than deposits. Redistributive fiscal policy can mitigate or offset the impact on net income, however. Casiraghi et al. (2016) use the Banca d’Italia quarterly model of the Italian economy (BIQM) to simulate monetary policy impulses on a micro dataset of Italian households’ income and wealth. They find that the recent unconventional monetary policy measures of the ECB have produced a negligible effect on inequality in Italy. Finally, Ampudia et al. (2018) assess the impact of standard and non-standard monetary policy on inequality in the EA based on household survey data and find expansionary monetary policy to reduce income inequality. Expansionary policy hurts households with significant liquid assets by reducing their income from wealth. More importantly still, expansionary monetary policy raises labor income, which has benefitted in particular households without significant wealth. The increase in labor income of hand-to-mouth households has also reduced consumption inequality in the EA. This has occurred despite the observation by Dolado et al. (2018), based on US data, that expansionary monetary policy may raise income inequality among workers by increasing the wage premium for highly skilled.

A part of the empirical studies mentioned above takes a partial equilibrium view, notably regressions of inequality metrics on monetary policy indicators that control for factors that may depend on monetary policy in the shorter or longer term as well. Accounting for interactions between different parts of the economy in establishing the net effects of policy over different time
horizons is the strength of structural dynamic macroeconomic models. Gornemann et al. (2016), e.g., analyze distributional consequences of conventional monetary policy in a New Keynesian model with household heterogeneity in time preferences and skills. Monetary policy with a strong focus on employment stabilization helps "ordinary" households, but hurts asset owners by reducing economy-wide savings and asset prices in their model. Despite the advantage of capturing interactions and second-round effects, analysis of the distributional impact of monetary policy in structural dynamic macroeconomic models has only emerged in recent years. The early New Keynesian DSGE models built on the assumption of a representative household, which precluded income or wealth inequality in the household sector. Subsequent work has introduced forms of heterogeneity, notably along the dimensions of wealth endowment and access to financial markets to better match business cycle facts. Liquidity-constrained consumers (e.g., Galí et al. 2007) and credit-constrained households (e.g., Iacoviello 2005) are prominent examples. More recently, HANK models (e.g., Kaplan et al. 2018) have introduced richer income and wealth distributions. At present, the richer distribution comes with constraints on the complexity in other dimensions and on the possibility to estimate the model, however.

In light of the trade-off between a richer income and wealth distribution (HANK models), on the one hand, and additional complexity in other dimensions (notably the distinction between bonds of short versus long maturity in the modelling of QE, and the open-economy structure to include an exchange-rate channel of monetary policy) as well as model estimation, on the other hand, we restrict our analysis to a two-agent set-up with intertemporally optimizing asset owners (NLC) and hand-to-mouth (LC) households. Hence, our framework is a TANK model in the language of Debortoli and Galí (2018). To the best of our knowledge, the paper is the first to focus on relative income and wealth effects of QE in an estimated DSGE framework.

3. Model environment
Our analysis is undertaken in the two-region (EA and RoW) model of Hohberger et al. (2018), which introduces elements to study the effects of QE using the portfolio rebalancing approach. We motivate non-neutrality of QE through the imperfect substitutability between long-term and short-term government bonds as in e.g., Andrés et al. (2004), Chen et al. (2012), Harrison (2012), and Priftis and Vogel (2016).
The EA region in the model is a one-sector economy. Perfectly competitive firms produce the final good, combining domestic and foreign intermediate goods and (imported) energy inputs. Firms in the intermediate goods sector are monopolistically competitive and maximize the present value of dividends (at a discount factor larger than the risk-free rate). There are two types of households: NLC households, who hold financial assets (equity and bonds), and LC households, who have no financial wealth and live ‘hand-to-mouth’. Given the holding of corporate equity (generating dividends) and domestic and foreign bonds (generating interest income), NLC households are significantly income-richer than LC ones in the steady state of our model. NLC households use financial markets to insure against income volatility, while LC households cannot insure and therefore benefit more strongly from a stabilization of economic activity and wage income. Wages of households are set by monopolistic trade unions. The government levies taxes on consumption, labor, profits, and a lump-sum tax, and issues debt to finance expenditures on consumption, investment, and transfers. The model features a number of nominal and real frictions (prices, wages, labor and capital adjustment), which are important to match business cycle properties.

In view of the limitation to focusing on NLC versus LC households, our model lends itself to an analysis of income inequality based on labor income and asset returns (as well as redistribution through fiscal policy) rather than an assessment of wealth inequality. Regarding the latter, any increase (decline) in value of the NLC asset position implies an increase (decline) in wealth inequality, given that LC households have zero financial wealth.

In what follows, we outline the elements of the model that are specific to the investigation of the distributional effects of conventional monetary policy and QE.¹

### 3.1 Distributional effects of monetary policy

The literature has discussed a number of channels through which monetary policy may affect inequality.² Our model captures the following elements: The income composition channel is present insofar as the two types of households have distinct income sources, and income from these sources varies in response to monetary policy. The portfolio channel is present, as expansionary monetary policy tends to increase the value of bonds and equity held by asset owners. The model also includes the counteracting effect that higher inflation in response to expansionary policy lowers

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¹ The outline neglects shocks and adjustment costs that are not crucial for the description. For a detailed overview of the model see Hohberger et al. (2018).
² For a discussion of the main distributional channels of monetary policy see Coibion et al. (2017).
the real value of nominal wealth. There are elements of the savings redistribution channel. Notably, exchange rate adjustment affects the real value of the net foreign asset position and the associated interest payments; inflation affects the real value of government debt, where interest income goes to asset owners, whereas tax liabilities affect all households. The model also features a form of the financial segmentation channel in that the LC households do not have access to financial markets. Notably, our model does not capture an earnings heterogeneity channel (e.g., through sectoral or skill differentiation) as wage and employment levels are the same for the two groups of households.

3.2 NLC households
The estimated value for the share of NLC households in our model (0.82) is in line with survey evidence in Ampudia et al. (2018) that 77% of EA households have significant liquid assets, and can hence reallocate portfolios. Kaplan et al. (2014) report quantitatively similar population shares for the remainder of LC households for a number of Western countries, namely approximately 20% for the US, approximately 20% or less for Australia, France, Italy, and Spain, and approximately 30% for Canada, the U.K., and Germany.

NLC households’ preferences are given by the infinite horizon expected life-time utility:

\[ U = E_0 \sum_{t=0}^{\infty} \bar{\beta}_t u_t(.) \]  

with \( \bar{\beta}_t = \beta \exp(\varepsilon_t^{C}) \), where \( \beta \) is the (non-stochastic) discount factor and \( \varepsilon_t^{C} \) captures a shock to the subjective rate of time preference (saving shock). They enjoy utility from consumption, \( C_{t}^{NLC} \), and incur disutility from labor, \( N_{t}^{NLC} \). The instantaneous utility function of NLC households is defined as:

\[ u(C_{t}^{NLC}, N_{t}^{NLC}) = \frac{1}{1-\theta}(C_{t}^{NLC} - h C_{t-1}^{NLC})^{1-\theta} - \frac{\omega^N}{1+\theta^N} (C_{t})^{1-\theta} (N_{t}^{NLC})^{1+\theta^N} \]  

where \( h \in (0; 1) \) measures the strength of external habits in consumption, and \( \omega^N \) is the weight of the disutility of labor.

The real period \( t \) budget constraint of NLC households, expressed relative to GDP deflator \( P_t \), is:

3 As there is no direct borrower-lender relationship between hand-to-mouth households and asset holders, there is no direct redistribution between domestic private debtors and lenders, which is otherwise a key element of the savings redistribution channel (Doepke and Schneider, 2006).

4 Williamson (2009) discusses a stricter form of the financial segmentation channel distinguishing between different classes of financial investors.
\[
\frac{(1+\tau^C)P_t^C}{\omega P_t}C_t^{NL_C} + \frac{B_t^S}{\omega(1+i_t)P_t} + \frac{P_t^{N B_L H}}{\omega P_t} \left( 1 + \frac{\gamma_b}{2} \left( k \frac{B_t^S}{B_t^{L H}} - 1 \right)^2 \right) + \frac{e_t B_t^W}{\omega(1+i_t^W)P_t} + \frac{\gamma_f}{2} \left( \frac{e_t (B_t^W - B_t^W)}{P_t Y_t} \right)^2 + \\
\frac{P_t^S S_t}{P_t} + \frac{TAX_t^{N LC}}{P_t} = (1 - \tau^N) \frac{W_t}{P_t} N_t^{NL_C} + \frac{B_t^{S_1}}{\omega P_t} + \frac{c + \delta_b \pi^N_t}{\omega P_t} B_t^{L H} - \frac{e_t B_t^W}{\omega P_t} + \left( \frac{P_t^S + d_t^t P_t^Y}{P_t} \right) S_{t-1} + \frac{T_{NL_C}^t}{\omega P_t}.
\]

(3)

NLC households consume, \( C_t^{NL_C} \), invest in short-term, \( B_t^S \), and long-term government bonds, \( B_t^{L H} \), foreign bonds, \( B_t^W \), corporate shares, \( S_t \), and pay taxes on consumption, labor income, and in a lump-sum way (\( \tau^C \), \( \tau^N \) and TAX\(_t^{NL_C} \)), respectively.\(^5\) They receive labor income, \( W_t N_t^{NL_C} \), coupon payments on the long-term bonds, \( c \) (defined below), dividends on corporate shares, \( d_t \), and interest income on short-term bonds, \( i_t \), and foreign bonds, \( i_t^W \), which are the differences between the notional value and the price at issuance. \( e_t B_t^W/(1 + i_t^W) \) is the price in domestic currency of a foreign bond, where \( e_t \) is the nominal exchange rate as the value in domestic currency of one unit of foreign currency. NLC households face an adjustment cost of holding foreign bonds, \( \gamma_f \), which captures a debt-dependent risk premium on foreign assets to ensure long-run stability (see Schmitt-Grohé and Uribe, 2003). \( P_t^C \) is the price of the consumption good. The dividends paid by intermediate good firms to shareholders are

\[
d_t = (1 - \tau^K) \left( Y_t - \frac{W_t}{P_t} N_t \right) + \tau^K \delta_{k_t} \frac{p_t^I}{P_t} K_{t-1} - \frac{p_t^I}{P_t} I_t - adjf^k_t,
\]

which is after-tax (\( \tau^K \)) corporate profit, i.e. turnover minus wage costs plus the capital depreciation allowance, net of investment expenditure (\( p_t^I I_t \)) and capital-stock adjustment costs (\( adjf^k_t \)). The gross nominal return on equity \( (1 + i_t^S) \) can be defined as the combination of dividend payments and the change in share value, i.e.

\[
1 + i_t^S = (p_t^S + d_t^t P_t^Y) / P_{t-1}^S.
\]

### 3.3 Imperfect substitutability between short-term and long-term bonds

The total outstanding government debt consists of long-term bonds, \( B_t^{L H} \), held by the private sector, \( B_t^{L CB} \), and the central bank, \( B_t^{L CB} \), and short-term bonds, \( B_t^S \). The price in period \( t \) of a short-term (1-period) bond of nominal value, \( B_t^S \), is \( B_t^S / (1 + i_t) \), with \( i_t \) being the short-term nominal interest rate. Long-term government debt is modelled as in Woodford (2001) as perpetuity that pays a nominal coupon, \( c \), which depreciates every period at the rate \( \delta_b \). The price in period \( t \) of a long-term bond, \( P_t^N \), issued in \( t \) equals the discounted value of future payments, \( P_t^N = \sum_{n=0}^{\infty} \frac{\delta_b^n}{(1+i_t)^{1+n}} C \),

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\(^5\) We divide the value of financial assets by the population share of NLC households, \( \omega \), to transform economy-wide per-capita values into values per NLC household member.
where $T$ is the maturity period of the bond. Short-term and long-term bonds are imperfect substitutes. In particular, NLC households target a mix of short-term and long-term bonds. Deviations from the target, $\kappa$, for the ratio of long-term to short-term debt induce quadratic adjustment costs, $\gamma_b$.

### 3.4 Portfolio rebalancing

NLC households maximize the present value of the expected stream of future utility subject to their budget constraint, by choosing the amount of consumption, $C_t^{NLC}$, and next period asset holdings, $B_t^S, B_t^{LH}, S_t, B_t^W$. Combining the first-order conditions (FOCs) with respect to $B_t^S$ with $C_t^{NLC}, S_t,$ and $B_t^W$, illustrates the transmission channels of monetary policy to the real economy in the model:

1. $\frac{1}{1+i_t} + \gamma_b \kappa P_t^N \left( \kappa \frac{B_t^S}{B_t^{LH}} - 1 \right) = \beta E_t \left( \frac{(1+r_{t+1}^{C})p_{t+1}^C u'(C_t^{NLC})}{(1+r_{t+1}^{C})p_{t}^C u'(C_t^{NLC})} \right) (4)$
2. $\frac{1}{1+i_t} + \gamma_b \kappa P_t^N \left( \kappa \frac{B_t^S}{B_t^{LH}} - 1 \right) = E_t \left( \frac{P_t^S - \beta^W}{P_{t+1}^S + d_{t+1}} \right) (5)$
3. $\frac{1}{1+i_t} + \gamma_b \kappa P_t^N \left( \kappa \frac{B_t^S}{B_t^{LH}} - 1 \right) = E_t \left( \frac{e_t}{e_{t+1}} \left( \frac{1}{1+i_t^W} + \gamma_f e_t \frac{B_t^W - \beta^W}{P_t Y_t} \right) \right) (6)$

The effects of a conventional monetary policy shock work in a standard fashion through the direct impact that the change in the short-term interest rate has on macroeconomic variables. An expansionary monetary policy shock leads to a reduction in savings (eq. 4), an increase in the prices of corporate equity (eq. 5), and an increase in the demand for foreign-currency denominated bonds, which leads to depreciation of the domestic currency (eq. 6).

The impact of QE on asset prices derives from the NLC households’ portfolio adjustment costs. If $\gamma_b > 0$, the effects of falling $B_t^{LH}$ relative to $B_t^S$ in the household portfolio, as the central bank purchases long-term bonds, are similar to the impact of a reduction of the short-term interest rate, $i_t$. Hence, QE can mimic the effects of a lower short-term interest rate on aggregate variables.

When the central bank purchases long-term bonds, NLC households, aiming to re-establish the portfolio mix of short-term and long-term bonds, can respond by investing in equity and foreign bonds, and by reducing savings. For given levels of the short-term rate, QE reduces private saving (eq. 4), triggers portfolio reallocation from government bonds towards corporate equity (eq. 5), and leads to higher demand for foreign assets, which depreciates the domestic currency (eq. 6).

Concerning the transmission to the real economy, (i) lower savings imply a substitution away from future consumption and towards contemporaneous consumption demand, (ii) rising stock markets
lead to stronger investment and capital accumulation, and (iii) exchange rate depreciation strengthens net exports if export demand and import demand are sufficiently price elastic.

3.5 Other channels of quantitative easing

The impact of conventional expansionary monetary policy and QE on portfolio allocation in the model has implications for consumption and investment that are similar to those of an extension of credit. First, financial intermediaries may face a similar decision problem as NLC households in our set-up. When the central bank buys long-term government bonds from banks, the latter can respond by buying more equity and foreign assets, and by providing more loans to firms.

Second, expansionary monetary policy can raise the net worth of banks and extend their lending margin in the presence of capital-requirement or equivalent constraints, as in, e.g., Gertler and Karadi (2011). Notably, Ricci (2015) finds that banks are more sensitive to non-standard measures than to interest rate decisions.

Moreover, financial investors in our model can also be interpreted to include pension and investment funds that act on behalf of households. Boubaker et al. (2018) provides evidence for portfolio rebalancing among institutional investors in form of a substantial increase in pension funds’ allocation to equity assets during the US Fed’s unconventional monetary policy measures. Our framework abstracts from the risk-taking channel of monetary policy. The risk-taking channel argues that investment strategies of financial investors may involve a “search for yield” through a demand for risky, tail-risk sensitive and illiquid securities (Rajan, 2006; Borio and Zhu, 2012) in a low interest rate environment (either through conventional policy or QE). The risk-taking channel of monetary policy has been shown to exist both in the US and in the EA. For the US, Bekaert et al. (2013) find a causal relationship between lax (conventional) monetary policy and increased risk appetite in financial markets. In addition, lower interest rates have been shown to result in reduced lending standards (Delis and Kouretas, 2011; Maddaloni and Peydro, 2011), higher leverage (de Groot, 2014) as well as increased asset risks (Angeloni et al., 2015). For the EA, expansionary monetary policy is associated with an increase in the willingness of banks to accept risk (Altunbas et al., 2014; Jimenez et al., 2014) and with lower lending standards (Neuenkirch and Noeckel, 2018).

The risk-taking channel constitutes an additional transmission mechanism for monetary policy, but its distributional implications for financial investors versus hand-to-mouth households are not
obvious. While "search for yield" may imply higher asset returns and valuation effects, potentially beneficial effects on corporate investment, output and employment would also benefit non-investor households through the labor income channel. Regarding distributional effects, the risk-taking channel may, hence, be similar to the portfolio rebalancing channel (combined with increased risk appetite) which we focus on in this paper.

Finally, an additional channel is that of investor sentiment (Lutz, 2015), i.e. that expansionary monetary policy leads to increased investor confidence/sentiment. This channel is partially captured in our model as far as expansionary monetary policy is likely to improve the economic outlook, which in turn affects investment decisions by forward-looking agents.

3.6 Conventional monetary policy and QE

Conventional monetary policy, as the first case, is described by a Taylor rule, where the central bank sets the short-term policy rate \( i_t \) in response to inflation and the output gap. The policy rate reacts sluggishly to deviations of inflation from its respective target level and to the output gap, and it is subject to random shocks:

\[
i_t - \bar{i} = \rho^i (i_{t-1} - \bar{i}) + (1 - \rho^i) \left( \eta^{in} (0.25 (\sum_{t=0}^{3} \pi_{t-r}^c) - \bar{\pi}^c) + \eta^{iy}(\bar{y}_t) \right) + u_{t}^{inom}
\]

where \( \bar{i} = r + \pi^c \) is the steady-state nominal interest rate, equal to the sum of the steady-state real interest rate and steady-state CPI inflation. \( \bar{y}_t \equiv \log(Y_t) - \bar{y}_t \) is the output gap with \( \bar{y}_t \) as (log) potential output. It is assumed that the risk-free rate is equal to the policy rate. A monetary policy shock in the conventional setting is therefore a shock to the exogenous component of the Taylor rule, \( u_{t}^{inom} \).

QE, as the second case, implies an increase in the central bank’s holding of longer-maturity assets. In the context of the European public-sector purchase program (PSPP), which accounts for most of the ECB’s QE measures since 2015, the central bank purchases long-term government bonds (\( B_{L,}^{CB} \)) and provides additional liquidity to the private sector. The operating profit of the central bank equals the sum of base money issuance and interest income minus the current expenditure on buying long-term bonds, where the latter equals the change of the value of long-term bonds on the central bank’s balance sheet:

\[
P_R_t^{CB} = \Delta M_t + c_{B_{t-1}^{L,}CB} - (P_t^{N} B_{t}^{L,}CB - B_{t-1}^{L,}CB)\]

(8)
We focus on the situation where the central bank engages in QE under an (endogenously) binding ZLB constraint. A binding ZLB implies that the target (‘shadow’) short-term policy rate is below the lower bound. An increase in output and inflation achieved by QE or other factors does not lead to tightening of the short-term rate as long as the ZLB is binding. As in Hohberger et al. (2018), we treat the occasionally binding ZLB via a piecewise linear solution. We employ the OccBin method developed by Guerrieri and Iacoviello (2015) and complement it with an algorithm by Giovannini and Ratto (2018) to obtain smoothed estimates of latent variables as well as the sequence of binding regimes along the historical sample.

In the case of conventional monetary policy, the endogenous part of the unconstrained nominal short-term interest rate \( i_t^{NC} \) follows the Taylor rule in equation (7) without monetary shock \( u_t^{inom} \). As long as the actual policy rate \( i_t \) is above the lower bound, it can be expressed as:

\[
i_t = i_t^{NC} + u_t^{inom}
\]

If \( i_t^{NC} \leq i_t^{LB} = 0 \), the policy rate is constrained:

\[
i_t = i_t^{LB} + u_t^{inom}
\]

The variable \( i_t^{NC} \) acts as the ‘shadow’ interest rate under a constrained regime. The algorithm by Giovannini and Ratto (2018) allows determining endogenously the duration of an occasionally binding constraint (see Hohberger et al., 2018).

### 3.7 Measuring the distributional impact of monetary policy

In order to assess the distributional impact of monetary policy we construct measures of household income and wealth positions and trace the responses of these statistics to standard monetary policy and quantitative easing shocks.

**Net disposable income of LC households:** Net disposable income of the ‘hand-to-mouth’ households is the sum of net wage income and transfer income minus lump-sum taxes:

\[
(1 - \tau^N)W_t N_t^{LC} + TR_t^{LC} - TAX_t^{LC}
\]

**Net disposable income of NLC households:** Net disposable income of the asset owners is the sum of net wage income, interest income from short-term government bonds, coupon payments on long-term government bonds, interest income on the foreign-currency denominated bond, dividend income on equity, and transfer income minus lump-sum taxes:
\[ (1 - \tau^N) W_t N_{t}^{LC} + \frac{l_t}{1 + l_t} \frac{B_t^S}{\omega} + e \frac{B_t^{C,H}}{\omega} + \frac{i_t^W}{1 + i_l} e_t \frac{B_t^W}{\omega} + d_t \frac{P_t^Y}{\omega} S_{t-1} + TR_t^{NLC} - T\lambda_t^{NLC} \] (10)

Net asset position of NLC households: The net asset position of asset holders at the beginning of period \( t \) equals the value of holdings of short-term and long-term government bonds, net foreign-currency denominated bonds, corporate equity, and money:

\[ \frac{B_t^{S-1}}{\omega} + \delta_p \frac{P_t^N}{\omega} \frac{B_t^{C,H}}{\omega} + e \frac{B_t^{W-1}}{\omega} + \frac{P_t^Y}{\omega} S_{t-1} + M_{t-1} \] (11)

When discussing income inequality (Section 4), we will emphasize the response of LC (NLC) disposable income relative to average disposable income in the economy. In the context of our two-household model, the relative per-capita income is a simpler metric than, e.g., the Gini coefficient, which measures the concentration of income or wealth along a continuum of heterogeneous households. Concerning the wealth distribution, as already mentioned, any increase (decline) in the value of the NLC household asset portfolio constitutes an increase (decline) in wealth inequality in our model, given that LC households have zero financial wealth.

4. Econometric approach and model solution

We compute an approximate model solution by linearizing the model around its deterministic steady state. We calibrate a subset of parameters to match long-run data properties and estimate the remaining parameters using Bayesian methods. The observables employed in estimation are listed in the Data Appendix. The estimation uses quarterly data for the period 1999q1-2017q1. We also perform estimation on the subsample 1999q1-2014q4 to test the stability of parameter estimates, especially the adjustment cost (portfolio preference) parameter \( \gamma_b \), with respect to the implementation of QE. The model has been estimated using the slice sampler algorithm proposed by Neal (2003).

We calibrate the steady state of the model so that steady-state ratios of main economic aggregates (relative to GDP) match average historical ratios over the sample period (see Table B.1 in the Appendix). The EA steady-state ratios of private consumption and investment to GDP are set to 56% and 18%, respectively. The steady-state share of EA GDP in world GDP is 16%. The steady-state trade share \((0.5 \times \text{exports+imports})/\text{GDP}\) is set at 19% in the EA (excluding intra-EA trade), and the quarterly depreciation rate of capital is 1.4%. We set the steady-state government debt to 74% of annual GDP in the EA. The steady-state real GDP growth and inflation rates are set to
0.35% and 0.4% per quarter, respectively, and the effective rate of time preferences to 0.25% per quarter.

With respect to the QE model extension, we observe the ‘securities held for monetary policy purposes’ as proxy for long-term bond holdings by the ECB, the share of long-term debt in total government debt, and the current and 3-month-ahead swap rates on 10-year government bonds to calculate the implied expected period-on-period return on long-term bonds.\(^6\) We set the steady-state portfolio share of long-term to short-term government debt \((κ)\) to 0.916 in line with the average of outstanding EA government debt over the sample period. Since we use interest rates for bonds with residual maturity of 10 years in our quarterly model, the corresponding depreciation rate of long-term government debt \((δ_b)\) is 0.975.

It is crucial to identify the parameter on portfolio adjustment costs \((γ_b)\) accurately as this parameter determines the impact of QE on the spread between short-term and long-term bond yields in the model. We specify a prior distribution with a mean of 15/10000 and a standard deviation of 6/10000.\(^7\) This captures the range of changes in interest spreads between short and long-term bonds around the time of the ECB’s QE announcement.

We treat ECB QE as an AR(2) shock for which the estimated parameters provide a hump-shaped path of central bank holdings of long-term government debt. The AR(2) specification captures the expectation of a further expansion of the central bank balance sheet in the future, as announced by the ECB at the start of its PSPP.

For QE under the ZLB constraint, we calculate impulse response functions (IRFs) using the concept of generalized impulse response functions: We choose as starting point 2015q1, which is a period of constrained monetary policy according to the Giovannini and Ratto (2018) algorithm, and the official start of the PSPP. We shut off the QE shock and simulate the model with all remaining shocks. Then we perform simulations adding a QE shock equivalent to long-term bond purchases of 1% of steady-state quarterly EA GDP on impact. The difference between the two simulations provides the IRF of the QE shock under an occasionally binding constraint. The size of the simulated QE shock is illustratively calibrated and does not reflect the actual purchases of long-term bonds by the ECB.

\[^6\] This approach is consistent with our modelling assumption that agents are not obliged to hold long-term bonds to maturity, but can trade these bonds in the secondary market at each period in time instead.

\[^7\] We check the robustness of this prior by specifying an uninformative uniform distribution for \(γ_b\). In both cases the posterior estimate is well identified around 0.0007.
In order to render the aggregate effects of the conventional monetary policy shock comparable to those of the QE shock, we adjust the monetary policy rule to generate GDP effects that are comparable in magnitude and dynamics to the QE shock. Since the monetary policy shock is being estimated as a white noise shock, we harmonize the persistence of the policy paths by setting the interest rate smoothing parameter ($\rho_i$) to 0.95, which quantitatively mimics the short-run effects of the QE shock on GDP under a ZLB regime.

The posterior estimates of key model parameters for the EA are reported in Table B.2 in the Appendix. The posterior estimates are based on the linearized version of the model (without ZLB); they are also used for the solution with an occasionally binding constraint.

5. Distributional effects of monetary policy shocks

Figure 1 shows responses of EA macro aggregates and relative income and wealth to a standard monetary policy and a QE shock. Figure 2 provides a decomposition of the components of NLC household income as described in Section 2.7.

5.1 Conventional monetary policy

Following an expansionary conventional monetary policy shock, real GDP and inflation increase temporarily. The domestic currency depreciates in nominal terms, and the economy depreciates against the RoW also in real effective terms. Real wages and hours worked increase in response to growing demand for labor. The short-term real interest rate declines, which stimulates domestic demand. LC and NLC consumption increase, but the increase is more pronounced for LC households. This resonates with previous findings in the literature that more financially constrained households have a higher marginal propensity to consume (Baker and Yannelis, 2017; Blundell et al., 2006; Johnson et al., 2006; Zeldes, 1989).

The wage share declines on impact due to the only moderate increase in real wages and the delayed response of hours worked. The delay in wage adjustment is driven by the estimated strong real-wage inertia and leads initially to an increase in the profit share. The net income share of LC households relative to GDP declines initially with the decline in the wage share. The response of the LC income share turns positive in the medium term. In contrast, the response of the net income

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8 Across all Figures we do not report error bands accounting for estimation uncertainty, but note that all impulse response functions are statistically significant at the 95% confidence level.
share of NLC households does not turn positive after the initial decline, but reverts to baseline in the medium term.

The fact that both LC and NLC household disposable income relative to GDP decline in Figure 2 relates to the role of fiscal policy. While NLC households suffer from a decline in the wage share and benefit from a higher profit share (dividend payments) on impact, they are, in addition, exposed to falling interest income on short-term bonds and a declining share of government transfers in income (automatic stabilizers). The mirror image of falling household income to GDP is due to an increase in the government budget balance in the model.

**Figure 1: Impulse responses for expansionary short-term rate and QE shock**

Note: Time intervals on the x-axis are quarters; units on the y-axis are in per cent, except for inflation, interest rates, the wage share, income shares and the asset position (pp). The wage share, the income shares and the net asset position are expressed relative to quarterly nominal GDP.
5.2 Quantitative easing

The purchase of long-term government debt by the central bank reduces the amount of long-term debt held by NLC households. In light of the preference of NLC households for a maturity mix, the price of long-term bonds rises, and the expected return on long-term bonds consequently falls. The decline in the expected return on long-term bonds leads to portfolio rebalancing towards corporate equity and foreign assets, leading to higher investment and real effective depreciation of the domestic currency. The lower expected return on long-term bonds also reduces private savings, which leads to an increase in NLC consumption. Stronger domestic demand increases the demand for labor, which strengthens LC wage income and consumption. Stronger domestic demand and net exports imply an increase in real GDP and higher (demand-driven) inflation.

Figure 1 shows an initial fall in the wage share to GDP also for the QE shock. The wage share response turns positive in the medium term, however, as employment and real wages increase. The net income share of LC households declines on impact, but improves in the medium term in line with the wage share. The NLC net income share faces a persistent decline, which is driven primarily by lower income (coupon payments) on long-term bond holdings, as part of the stock is purchased by the central bank in return for interest-free money. The return on short-term bonds remains
unchanged in the short run due to the ZLB constraint, but increases in the medium term as the (shadow) interest rate endogenously exits the constraint and becomes positive.

5.3 *Income and wealth inequality*

A metric to assess the impact of shocks on *income* inequality more directly is the per-capita disposable income of LC and NLC households relative to the average per-capita disposable income in the economy. Figure 3 shows the responses of the relative LC (NLC) net disposable income, i.e. LC (NLC) per-capita disposable income relative to the population average, for the conventional monetary policy and QE shocks in Figures 1 and 2. Both shocks have qualitatively identical effects. The LC disposable income in relative terms slightly declines on impact, but then increases quickly to above baseline and persistently remains above baseline in the medium and longer run. The NLC net income in relative terms increases slightly on impact, but then falls below baseline and persistently remains below baseline in the medium and longer run.⁹

![Figure 3: Dynamic of disposable household income relative to the economy-wide average](image)

Note: Time intervals on the x-axis are quarters. The income shares measure the respective household (LC vs NLC) disposable income (after taxes and transfers) relative to the economy-wide average household disposable income and are expressed in percentage-point deviations from the baseline.

The relative income responses are driven by the response of wage income versus income on financial assets. Higher employment and real wages in response to expansionary monetary policy lead to higher labor income. Higher labor income benefits especially the LC households, given that

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⁹ Changes in LC and NLC income relative to the average household income in the economy move, by definition, in opposite direction. The LC versus NLC percentage-point changes differ, however. NLC households represent a larger share of the population according to our estimates. A given absolute change in income therefore implies a more pronounced change in average LC household income compared to average NLC household income. LC and NLC income effects add up to zero when adjusted for LC and NLC population shares.
wages are their only source of primary revenue. NLC households also receive higher wage income, but at the same time see the contribution of dividend payments and income on financial investment decline in relative terms (Figure 2). In the case of the conventional monetary policy shock, interest income from holding short-term government bonds declines. In the case of the QE shock, NLC households face a decline in their long-term bond position, which implies a loss in income from coupon payments. For monetary policy shocks with similar initial impact on aggregate GDP, the loss of coupon payments (QE) is quantitatively more important than the decline in interest received on short-term bonds (conventional policy shock), which explains the larger changes in the LC versus NLC income shares in the case of QE. For a QE shock that generates around 0.1% initial increase in real GDP, a change in relative per-capita income by more than 0.1 percentage points for LC households is not negligible in quantitative terms. The relative income effect for a comparable expansionary shock to the short-term rate (Taylor rule) is much smaller instead. The relative income responses for LC and NLC households are in line with the finding in Ampudia et al. (2018) for the EA that expansionary monetary policy reduces household income inequality and that positive employment and wage responses are an important driver of this result.

5.4 Discussion

Given our two-household model set-up with NLC asset-owner versus zero-asset LC households, any increase (decline) in the NLC portfolio value corresponds to increasing (declining) wealth inequality. The expansionary monetary policy shocks raise the value of financial assets on impact, so that the net asset position of NLC households increases in terms of domestic GDP. The valuation effect in response to the conventional monetary policy shock remains temporary and recedes as the monetary shock decays. The effect is not negligible in quantitative terms, however. The short-term response of NLC wealth to the QE shock is quantitatively very similar to the response to conventional monetary policy shocks. Instead of returning to baseline however, the net wealth of NLC households falls below baseline in the medium and long term in response to the QE shock. The negative wealth effect derives from the loss of coupon payments, which is a consequence of the NLC households’ reduced holding of long-term bonds. The persistent fall in bond returns (coupon payments) leads to a decumulation of NLC assets compared to baseline in the medium and longer term. Overall, the impulse responses suggest that temporary expansionary conventional monetary policy and QE shocks may reinforce wealth inequality temporarily on
impact, without implying persistent increases in wealth inequality between asset owners and households without (liquid) assets.

5.5 Actual volumes of quantitative easing

Since the model does not lead to transition to a new steady state for real variables in response to temporary monetary policy shocks, changes in income shares and inequality are temporary and decay in the long term. To illustrate the impact of QE volumes of the magnitude of the ECB program over the medium term, we conduct a deterministic experiment where we replicate the path of bond purchases by the central bank in the context of the PSPP.

Figure 4 illustrates the implied path of the QE policy considered. The deterministic shock lasts for three years. It has a hump-shaped pattern due to the AR(2) specification and a cumulative size of around 50% of annual EA GDP. While the expansion of the central bank’s balance sheet stops after four years, it remains extended for a long time, given the persistence in the shock profile.

![Figure 4: Simulated path of QE program](image)

Note: Time intervals on the x-axis are years; units on the y-axis are per cent of GDP.

Figure 5 shows the impact of the policy path on a selection of endogenous model variables. Given the deterministic setting, shock duration and size are known ex ante, i.e. anticipated by the private sector.

The effect on GDP is large and reflects the large volume of the QE program as well as its deterministic nature in the scenario. Since the assumption of perfect foresight implies front-loading of the QE effects, real GDP and consumer prices increase by 2% and 1.2% on impact, respectively. The effects of the implied QE path are persistent, with real GDP being 0.3% and consumer prices 6% above baseline after 10 years.
The impact on LC income as share of GDP is positive in the medium run, in line with the medium-term increase in the wage share, and reaches a size of 0.3% of nominal GDP compared to baseline after 10 years. NLC income to GDP falls, reaching a level of -1.2 percentage points below baseline after 10 years. The asset position of NLC households increases by 20% of nominal GDP on impact, but falls thereafter to less than 20 percentage points below baseline after 10 years. Both LC and NLC consumption increase in line with higher income. LC consumption rises more in per-cent terms, in line with the increasing LC income-to-GDP share.

Figure 5: Impact of the deterministic QE path

Note: Time intervals on the x-axis are years; units on the y-axis are in per cent (pp for inflation, interest rates, income shares and the asset position to GDP). Shares are expressed in per cent of annual nominal GDP.
6. Conclusion

This paper analyzes the distributional consequences of conventional monetary policy and QE using an estimated open-economy DSGE model of the EA and the RoW, with NLC (asset owners) and LC (‘hand-to-mouth’) households. The model includes imperfect substitutability between government bonds of different maturities and central bank balance sheet operations, and it compares impulse response functions from shocks to the Taylor rule (conventional monetary policy) and the central bank balance sheet (QE).

Overall, expansionary conventional monetary policy and QE shocks do not increase, but rather mitigate income and wealth inequality between population groups in our two-household model in the short (income) and medium (income and wealth) term. While the distinction between two household groups is certainly simplistic, it provides insight with respect to the functional income distribution and the dependence of income and wealth effects on income sources and financial market participation.
References


APPENDIX A: DATA

1. Data sources
Data for the EA (quarterly national accounts, fiscal aggregates, quarterly interest and exchange rates) are taken from Eurostat. ROW series are constructed on the basis of the IMF International Financial Statistics (IFS) and World Economic Outlook (WEO) databases.

2. Constructing of data series for ROW variables
Series for GDP and prices in the ROW starting in 1999 are constructed on the basis of data for the following 59 countries: Albania, Algeria, Argentina, Armenia, Australia, Azerbaijan, Belarus, Brazil, Bulgaria, Canada, Chile, China, Colombia, Croatia, Czech Republic, Denmark, Egypt, Georgia, Hong Kong, Hungary, Iceland, India, Indonesia, Iran, Israel, Japan, Jordan, Korea, Lebanon, Libya, FYR Macedonia, Malaysia, Mexico, Moldova, Montenegro, Morocco, New Zealand, Nigeria, Norway, Philippines, Poland, Romania, Russia, Saudi Arabia, Serbia, Singapore, South Africa, Sweden, Switzerland, Syria, Taiwan, Thailand, Tunisia, Turkey, Ukraine, United Arab Emirates, United Kingdom, United States, and Venezuela. The ROW data are annual data from the IMF International Financial Statistics (IFS) and World Economic Outlook (WEO) databases.

3. List of observables
The estimation uses the following time series for the EA: GDP, GDP deflator, population, total employment, employment rate, relative prices with respect to GDP deflator (VAT-consumption, government consumption, private investment, export, and import), government investment price relative to private investment, nominal policy rate, and nominal shares of GDP (consumption, government consumption, investment, government investment, government interest payment, transfers, public debt, wage bill and exports). The list of observables also includes the oil price and the effective exchange rate of the EA. For the ROW we use data on population, GDP, GDP deflator and the nominal policy rate. The EA specific QE observables are securities held for monetary policy purposes as proxy for long-term bond holdings by the ECB and the share of long-term debt in total government debt. Furthermore, we use current and 3-month-ahead swap rates on 10-year government bonds to calculate the implied expected period-on-period return on long-term bonds.
## APPENDIX B: CALIBRATION AND POSTERIOR ESTIMATES

### Table B.1: Calibrated parameters and steady-state ratios

<table>
<thead>
<tr>
<th>Description</th>
<th>Parameter or ratio</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Preferences</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intertemporal discount factor</td>
<td>0.9975</td>
<td>annual discount rate of 1%</td>
</tr>
<tr>
<td>Degree of openness</td>
<td>0.19</td>
<td>data</td>
</tr>
<tr>
<td>Substitutability btw domestic varieties</td>
<td>6.97</td>
<td>endogenized in steady state</td>
</tr>
<tr>
<td>Weight of disutility of labor</td>
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<td>endogenized in steady state</td>
</tr>
<tr>
<td><strong>Production</strong></td>
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<td></td>
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<tr>
<td>Cobb-Douglas labor share</td>
<td>0.65</td>
<td>standard share in literature</td>
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<tr>
<td>Depreciation of private and public capital</td>
<td>0.0144</td>
<td>data</td>
</tr>
<tr>
<td>Share of oil in total output</td>
<td>0.015</td>
<td>data</td>
</tr>
<tr>
<td><strong>Fiscal policy</strong></td>
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<tr>
<td>Consumption tax</td>
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<tr>
<td>Corporate profit tax</td>
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<tr>
<td>Labor tax</td>
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<td>endogenized in steady state</td>
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<td>Deficit target</td>
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<td>data</td>
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<tr>
<td>Debt target</td>
<td>2.96</td>
<td>data</td>
</tr>
<tr>
<td><strong>Steady state ratios</strong></td>
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<tr>
<td>Private consumption share</td>
<td>0.56</td>
<td>data</td>
</tr>
<tr>
<td>Private investment share</td>
<td>0.18</td>
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<tr>
<td>Gov’t consumption share</td>
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<tr>
<td>Gov’t investment share</td>
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<td>data</td>
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<tr>
<td>Transfers share</td>
<td>0.16</td>
<td>data</td>
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<tr>
<td><strong>Others</strong></td>
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<td></td>
</tr>
<tr>
<td>Size of the country (% of world)</td>
<td>16.44</td>
<td>data</td>
</tr>
<tr>
<td>Trend of total factor productivity</td>
<td>0.0033</td>
<td>data</td>
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### Table B.2: Prior and posterior distributions of key estimated EA model parameters

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<thead>
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<th>Description</th>
<th>Prior Distribution</th>
<th>Posterior Distribution</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Preferences</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Consumption habit persistence</td>
<td>B 0.5 (0.20)</td>
<td>0.90 (0.02)</td>
</tr>
<tr>
<td>Risk aversion</td>
<td>G 1.5 (0.20)</td>
<td>1.54 (0.17)</td>
</tr>
<tr>
<td>Inverse Frisch elasticity of labor supply</td>
<td>G 2.5 (0.50)</td>
<td>2.09 (0.44)</td>
</tr>
<tr>
<td>Import price elasticity</td>
<td>G 2 (1)</td>
<td>2.54 (0.28)</td>
</tr>
<tr>
<td>Steady state consumption share of NLC HH</td>
<td>B 0.65 (0.10)</td>
<td>0.82 (0.04)</td>
</tr>
<tr>
<td><strong>Nominal and real frictions</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Portfolio adjustment costs</td>
<td>G 0.0015 (0.0006)</td>
<td>0.0007 (0.0002)</td>
</tr>
<tr>
<td>Price adjustment cost</td>
<td>G 60 (40)</td>
<td>42.6 (9.25)</td>
</tr>
<tr>
<td>Nominal wage adj. cost</td>
<td>G 5 (2)</td>
<td>5.55 (1.48)</td>
</tr>
<tr>
<td>Real wage rigidity</td>
<td>B 0.5 (0.20)</td>
<td>0.97 (0.01)</td>
</tr>
<tr>
<td><strong>Monetary Policy</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Interest rate persistence</td>
<td>B 0.7 (0.12)</td>
<td>0.80 (0.03)</td>
</tr>
<tr>
<td>Response to inflation</td>
<td>B 2 (0.4)</td>
<td>1.61 (0.19)</td>
</tr>
<tr>
<td>Response to GDP</td>
<td>B 0.5 (0.2)</td>
<td>0.06 (0.02)</td>
</tr>
<tr>
<td><strong>Autocorrelations of shocks</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>QE AR(1) (purchases of long-term bonds)</td>
<td>N 1.8 (0.4)</td>
<td>1.75 (0.10)</td>
</tr>
<tr>
<td>QE AR(2) (purchases of long-term bonds)</td>
<td>N -0.8 (0.3)</td>
<td>-0.76 (0.09)</td>
</tr>
<tr>
<td>Bond risk premium</td>
<td>B 0.5 (0.20)</td>
<td>0.87 (0.05)</td>
</tr>
<tr>
<td>Domestic price mark-up</td>
<td>B 0.5 (0.20)</td>
<td>0.54 (0.13)</td>
</tr>
<tr>
<td><strong>Standard deviations (%) of innovations</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Monetary Policy</td>
<td>B 1 (0.40)</td>
<td>0.10 (0.01)</td>
</tr>
<tr>
<td>QE (purchases of long-term bonds)</td>
<td>G 1 (0.40)</td>
<td>1.12 (0.17)</td>
</tr>
<tr>
<td>Investment risk premium</td>
<td>G 0.1 (0.40)</td>
<td>0.30 (0.05)</td>
</tr>
<tr>
<td>Bond risk premium</td>
<td>G 1 (0.40)</td>
<td>0.17 (0.09)</td>
</tr>
<tr>
<td>Domestic price mark-up</td>
<td>G 2 (0.80)</td>
<td>4.46 (1.07)</td>
</tr>
</tbody>
</table>

Notes: Cols. (1) lists estimated model parameters and shocks. Cols. (2)-(3) indicates the prior distribution function (B: Beta distribution; G: Gamma distribution; N: Normal distribution). Cols. (4)-(5) show the mode and the standard deviation (std) of the posterior distributions of EA parameters.
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